

# **RB-OLITS: A Worst-case Reorder Buffer Size Reduction Approach for 3D-NoC**

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# Outline

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- **Background**
- Preliminaries
- Worst-case Size Reduction of Reorder Buffer
- Experiments and Results
- Conclusion

# Background

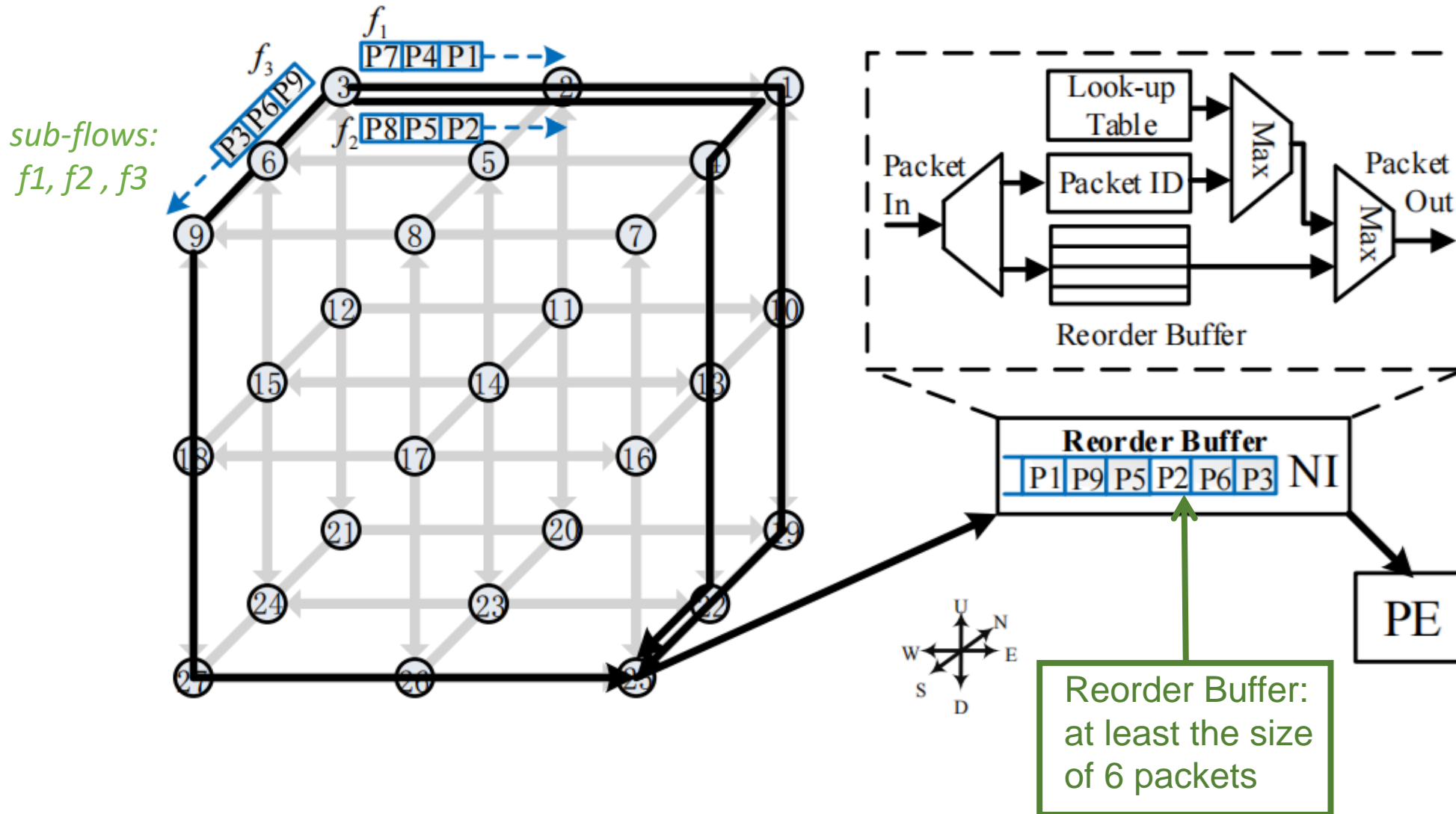
- **3D-NoC is emerging as a promising successor to the traditional bus-interconnecting architecture in MPSoC designs**
- **The packet based 3D-NoC paradigm is highly scalable and fundamentally decouples communication from computation**
- **In-order packet delivery is crucial for a majority of applications, for instance, multimedia or cache coherence protocols**
- **Packets arriving at the destination may cause the out-of-order problem**
- **Calculation and reduction of worst-case reorder buffer size has become a pivotal research topic.**

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# Preliminaries



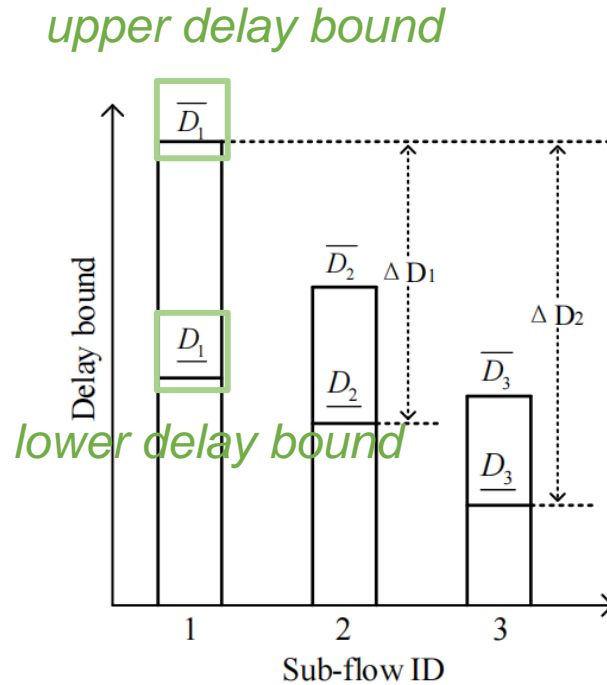
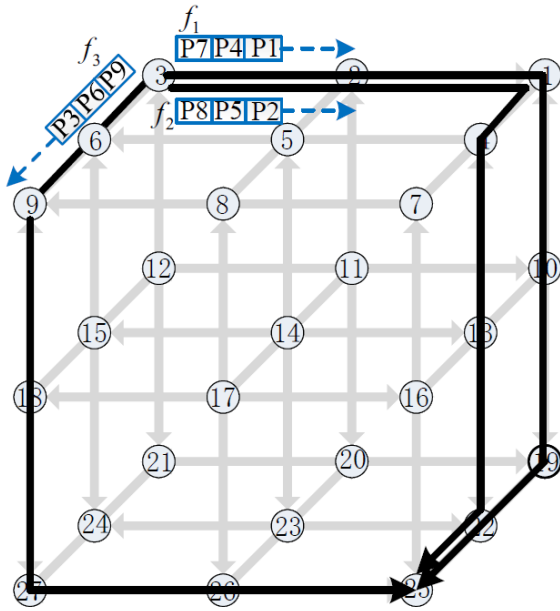
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# Worst-case Size Reduction of Reorder Buffer

## Motivating Example



$$S_{rb} = \frac{(\bar{D}_1 - \underline{D}_2)}{\Delta t_2} + \frac{(\bar{D}_1 - \underline{D}_3)}{\Delta t_3}$$

**generalize to n**

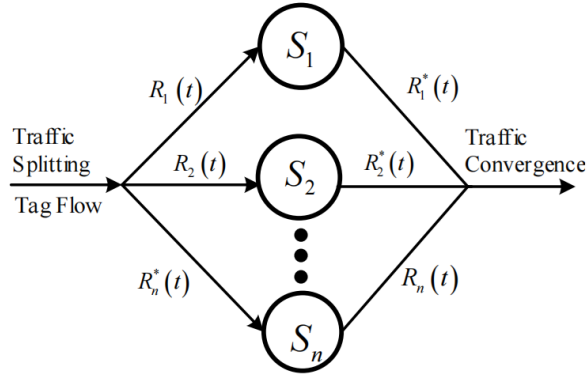
$$S_{rb}^{\max} = \frac{(\bar{D}_{\max} - \underline{D}_1)}{\Delta t_1} + \frac{(\bar{D}_{\max} - \underline{D}_2)}{\Delta t_2} + \dots + \frac{(\bar{D}_{\max} - \underline{D}_n)}{\Delta t_n}$$

$$\bar{D}_{\max} = \max\{\bar{D}_1, \bar{D}_2, \dots, \bar{D}_n\}$$

*the packet injection intervals*

# Worst-case Size Reduction of Reorder Buffer

## Worst-case Reorder Buffer Size Analysis Based on Network Calculus



**Step 1: Traffic splitting**

**Step 2: Equivalent service curve (ESC) and delay bound calculation**

**Step 3: Calculation of worst-case reorder buffer size**

$$\begin{aligned}
 S_{rb}^{max} &= \{R_m^*(t) - R_1^*(s)\} + \{R_m^*(t) - R_2^*(s)\} \\
 &\quad \dots + \{R_m^*(t) - R_n^*(s)\} \\
 &= \alpha_1^*(\Delta t_1) + \alpha_2^*(\Delta t_2) \dots + \alpha_n^*(\Delta t_n) \\
 &= \{r_1(\Delta t_1) + b_1 + r_1 T_1\} \\
 &\quad + \{r_2(\Delta t_2) + b_2 + r_2 T_2\} \\
 &\quad \dots + \{r_n(\Delta t_n) + b_n + r_n T_n\} \\
 &= \{r_1(h(\alpha_m, \beta_m) - D_1^{low}) + b_1 + r_1 T_1\} \\
 &\quad + \{r_2(h(\alpha_m, \beta_m) - D_2^{low}) + b_2 + r_2 T_2\} \\
 &\quad \dots + \{r_n(h(\alpha_m, \beta_m) - D_n^{low}) + b_n + r_n T_n\} \\
 &= \{r_1(T_m + \frac{b_m}{R_m} - D_1^{low}) + b_1 + r_1 T_1\} \\
 &\quad + \{r_2(T_m + \frac{b_m}{R_m} - D_2^{low}) + b_2 + r_2 T_2\} \\
 &\quad \dots + \{r_n(T_m + \frac{b_m}{R_m} - D_n^{low}) + b_n + r_n T_n\}
 \end{aligned}$$



# Worst-case Size Reduction of Reorder Buffer

## (1) Adjacency Matrix:

$$A = (a_{ij})_{v \times 6}$$

$$a_{ij} = \begin{cases} p_{ij}, & \text{splitting proportion in } j \text{ direction at node } v_i \\ 0, & \text{else} \end{cases}$$

## (2) Contention Matrix:

*flow rate and burstiness of sub-flow  $i$*

$$C_{s_i, d_i} = [(\varepsilon r_1 + \beta b_1) A_{s_1, d_1} + (\varepsilon r_2 + \beta b_2) A_{s_2, d_2} + \dots + (\varepsilon r_j + \beta b_j) A_{s_j, d_j} + \dots + (\varepsilon r_k + \beta b_k) A_{s_k, d_k}] \wedge A_{s_i, d_i}, j \neq i$$

*$\varepsilon$  and  $\beta$  are the impact factor of  $r_i$  and  $b_i$*

# Worst-case Size Reduction of Reorder Buffer

## (3) Congestion Factor:

*the total number of nodes in the sub-flow*

$$\lambda_{f_i} = \sum_{i=1}^N C(\text{node\_}i, \text{direction\_}j)$$

*the direction next to node i*

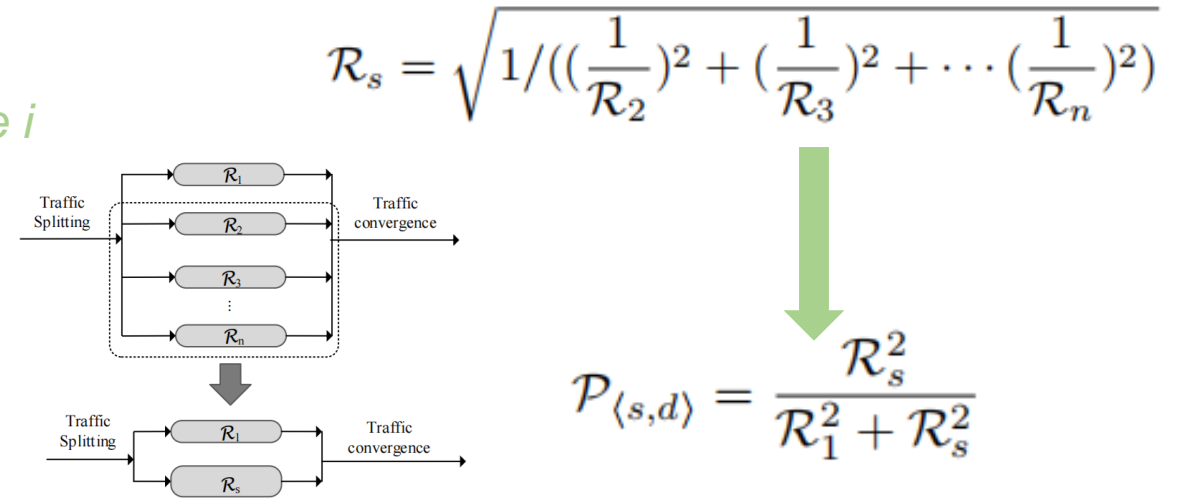
*the i-th node along the sub-flow*

## (4) RB-OLITS:

$$S_{rb}^{max} = \{r_1(T_m + \frac{b_m}{R_m} - D_1^{low}) + b_1 + r_1 T_1\}$$

$$+ \{r_2(T_m + \frac{b_m}{R_m} - D_2^{low}) + b_2 + r_2 T_2\}$$

$$\dots + \{r_n(T_m + \frac{b_m}{R_m} - D_n^{low}) + b_n + r_n T_n\}$$



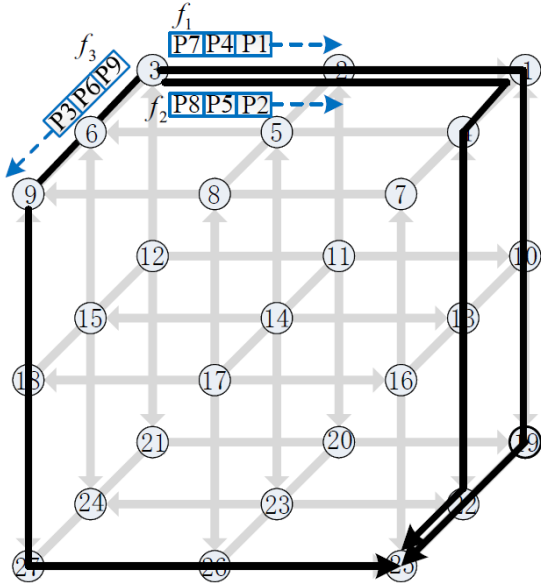
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- Worst-case Size of Reorder Buffer
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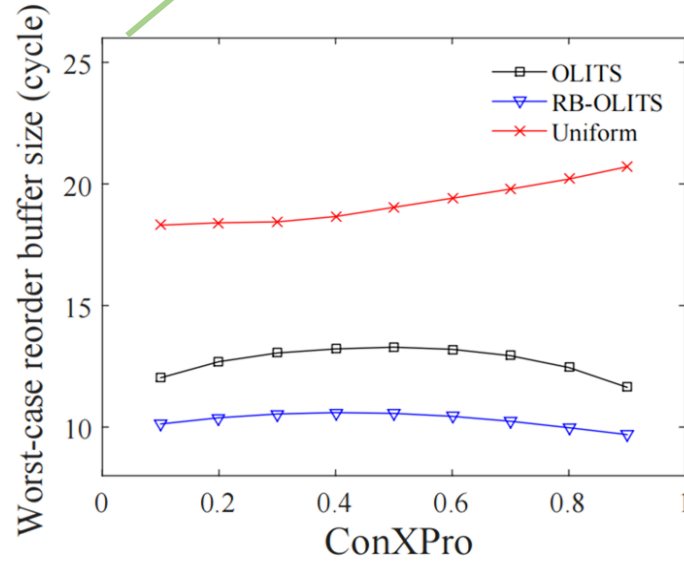
# Experiment and Result

## Synthetic Pattern



tag flow  
f(3, 25)

f(4, 20), f(8, 19), f(4, 23)



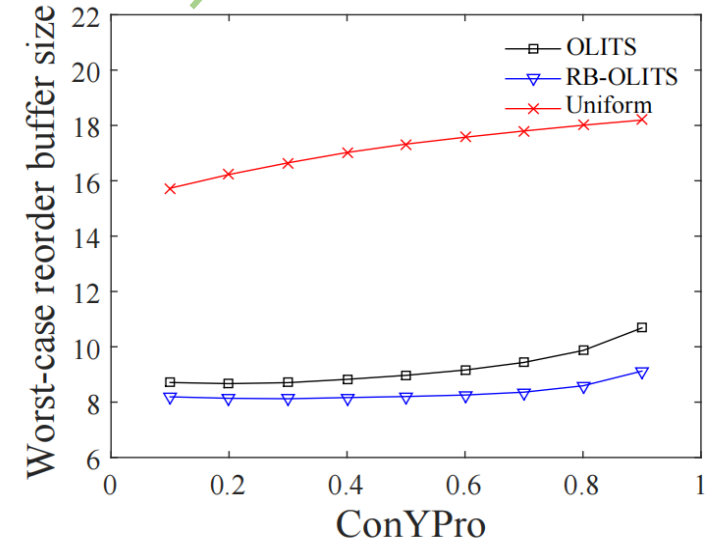
**vs. Uniform**

max: 53.20% average: 46.35%

**vs. OLITS**

max: 20.88% average: 19.09%

f(4, 20), f(8, 19)

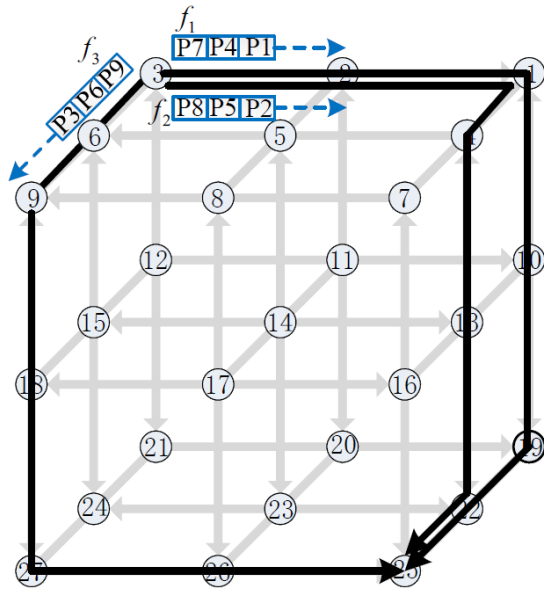


**vs. OLITS**

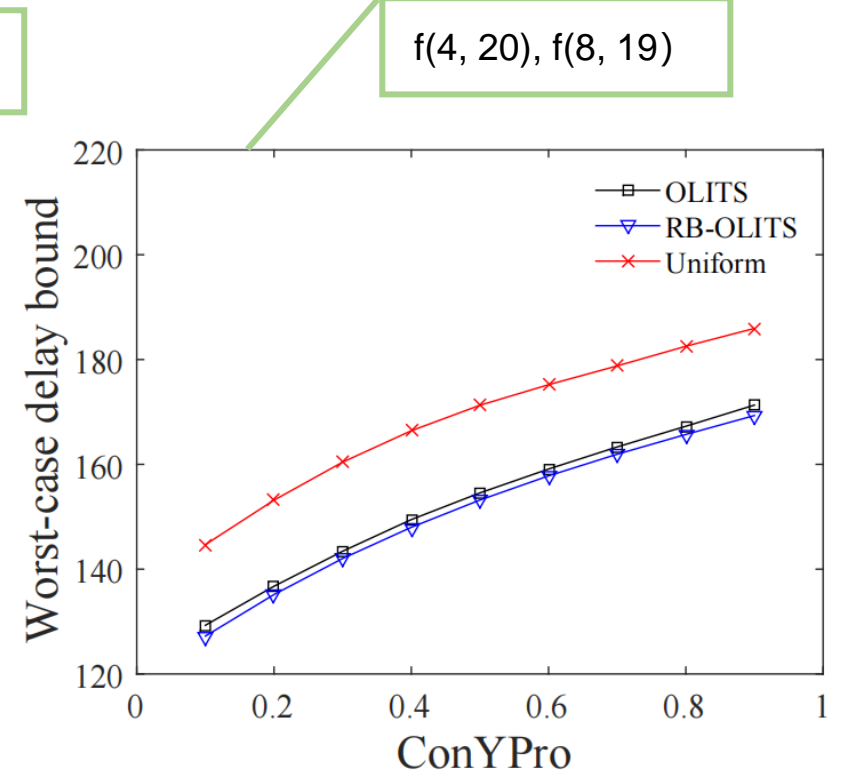
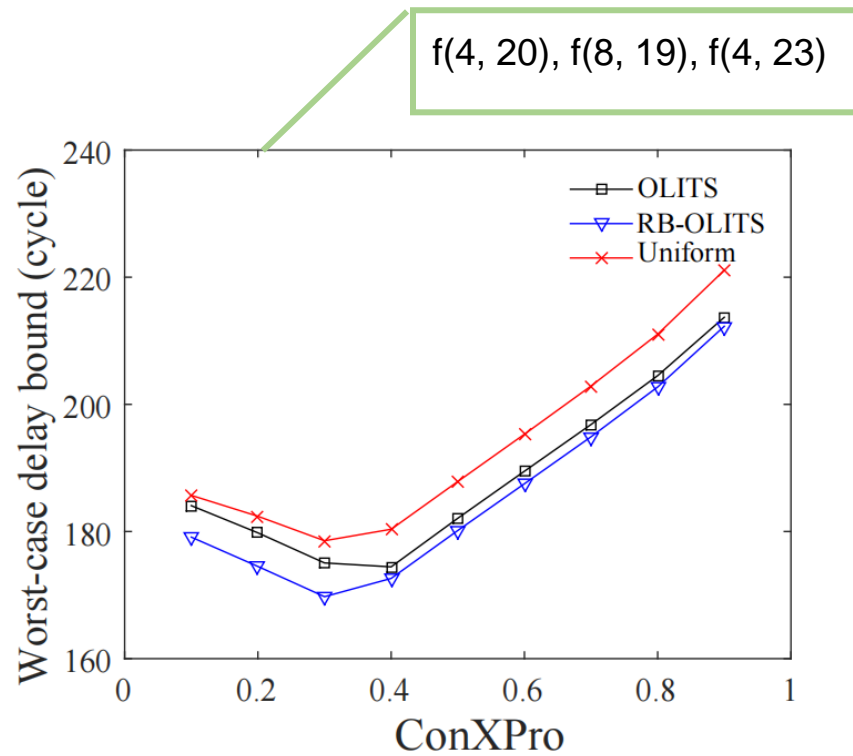
max: 14.60% average: 9.28%

# Experiment and Result

## Synthetic Pattern



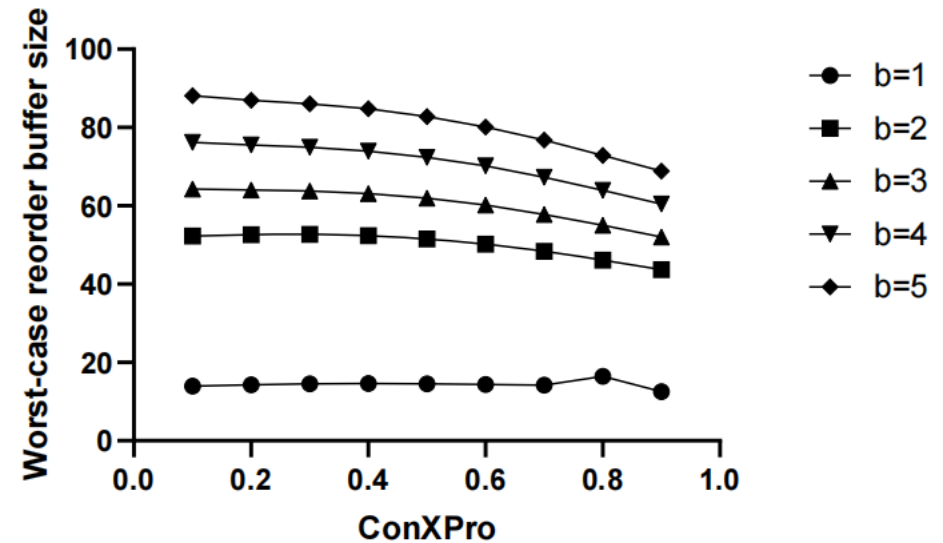
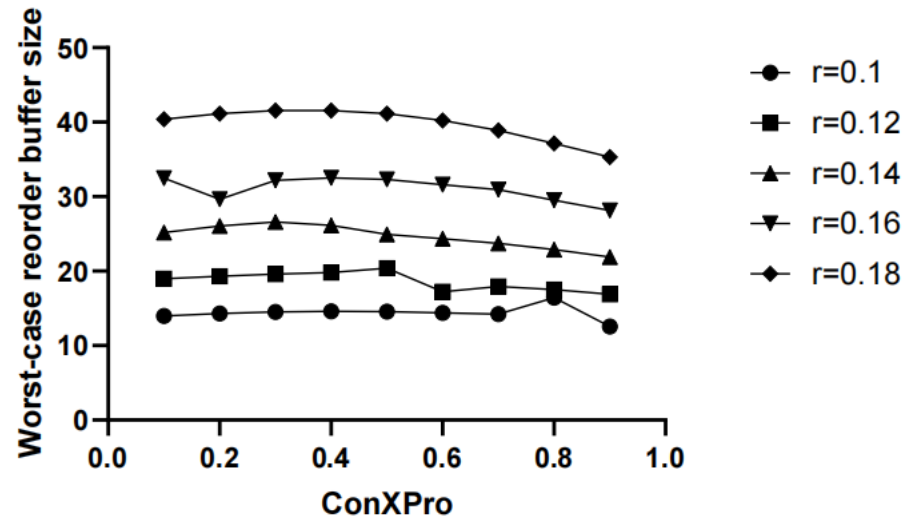
tag flow  
 $f(3, 25)$



# Experiment and Result

## Synthetic Pattern:

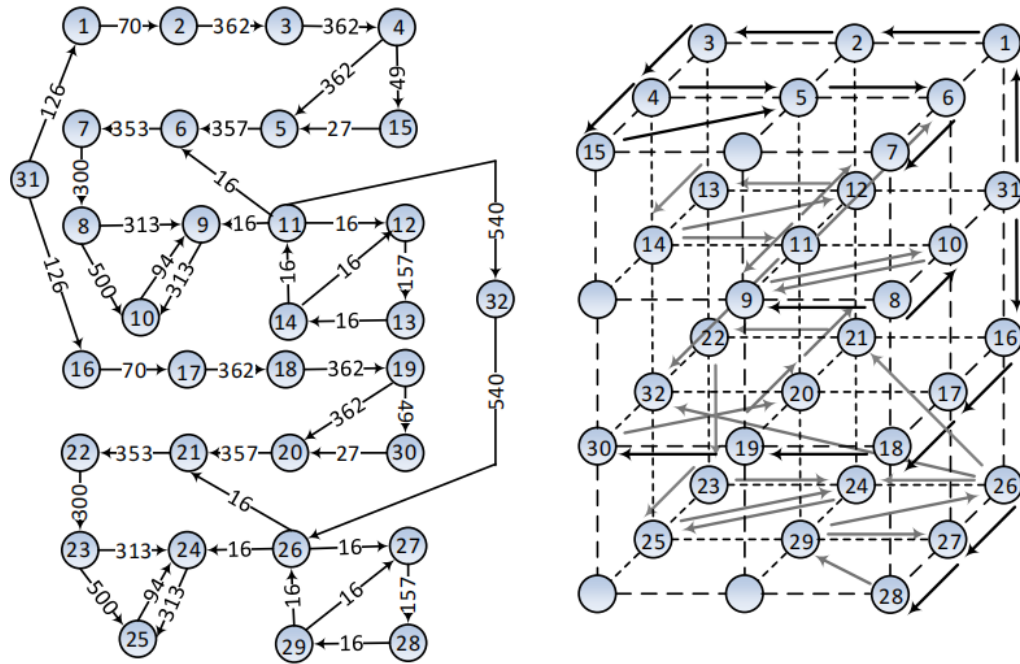
Impact of injection rate with varying bustiness



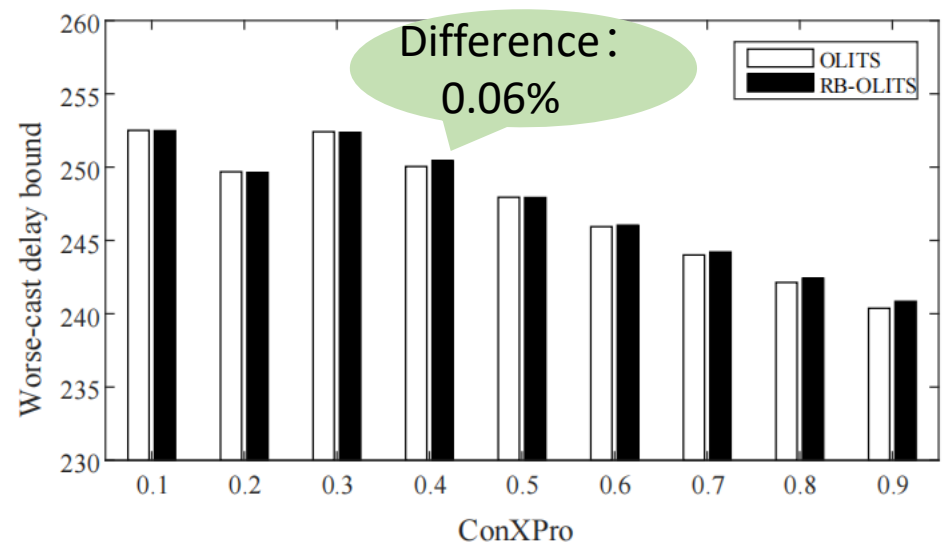
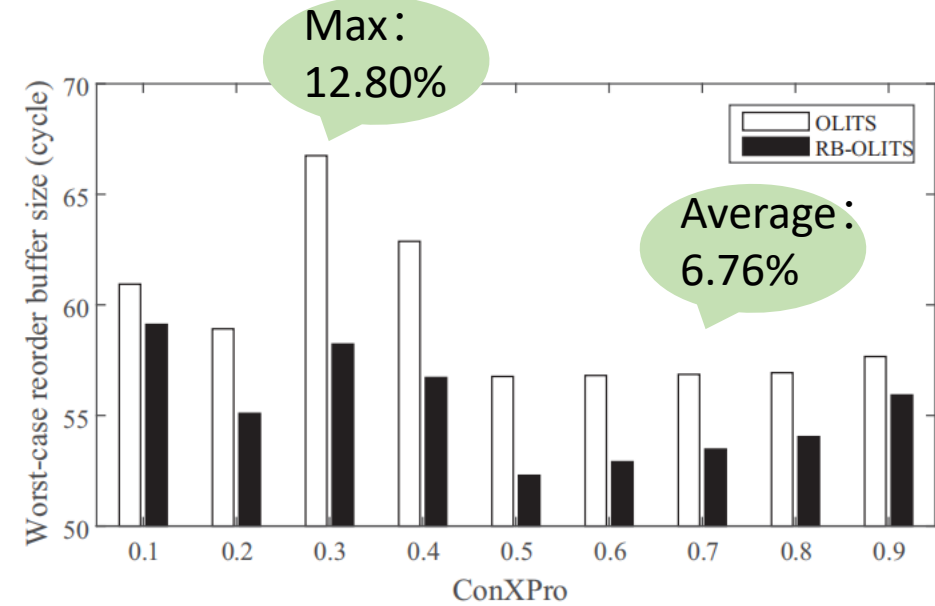
**With the increasing injection rate or burstiness, the worst-case reorder buffer size increases accordingly**

# Experiment and Result

## Industrial Pattern



43 contention flows  
 $\beta(t) = 0.33 \cdot (t - 3)^+$   
 12 sub flows



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# Conclusion

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■ **An analytical model for calculating the worst-case reorder buffer size for multi-path minimal routing 3D-NoCs using network calculus**

- support arbitrary number of sub-flows

■ **A traffic splitting method, named RB-OLITS, for reducing worst case reorder buffer size.**

- an improvement of 5.9%-20.9% in most cases

***Thank you!***